

Data-Intensive Distributed Computing

CS 451/651 (Fall 2018)

Part 6: Data Mining (1/4) October 25, 2018

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These slides are available at http://lintool.github.io/bigdata-2018f/



Structure of the Course

Analyzing Text

Analyzing Graphs

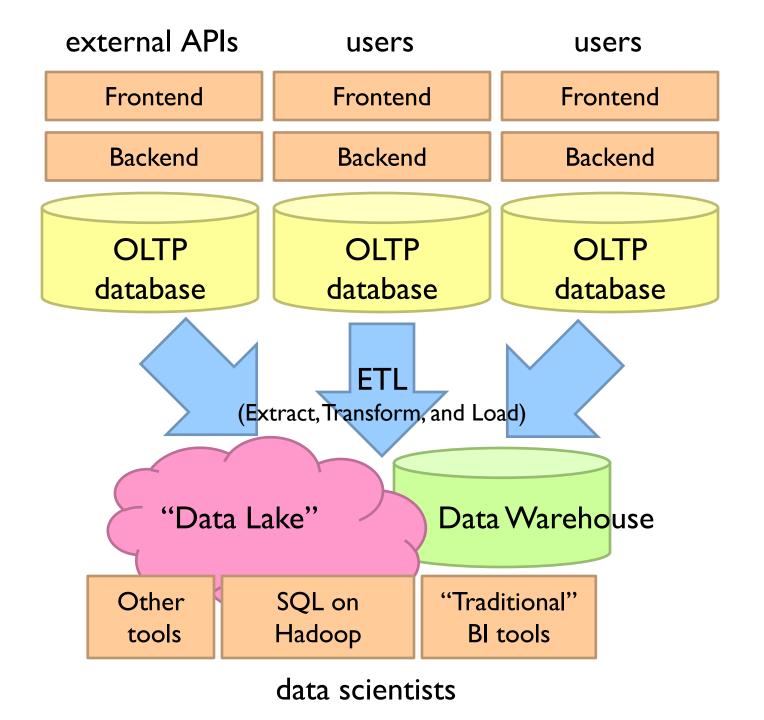
Analyzing Relational Data

Data Mining

"Core" framework features and algorithm design

Learn new buzzwords!

Descriptive vs. Predictive Analytics



Supervised Machine Learning

The generic problem of function induction given sample instances of input and output

Focus today

Classification: output draws from finite discrete labels

Regression: output is a continuous value

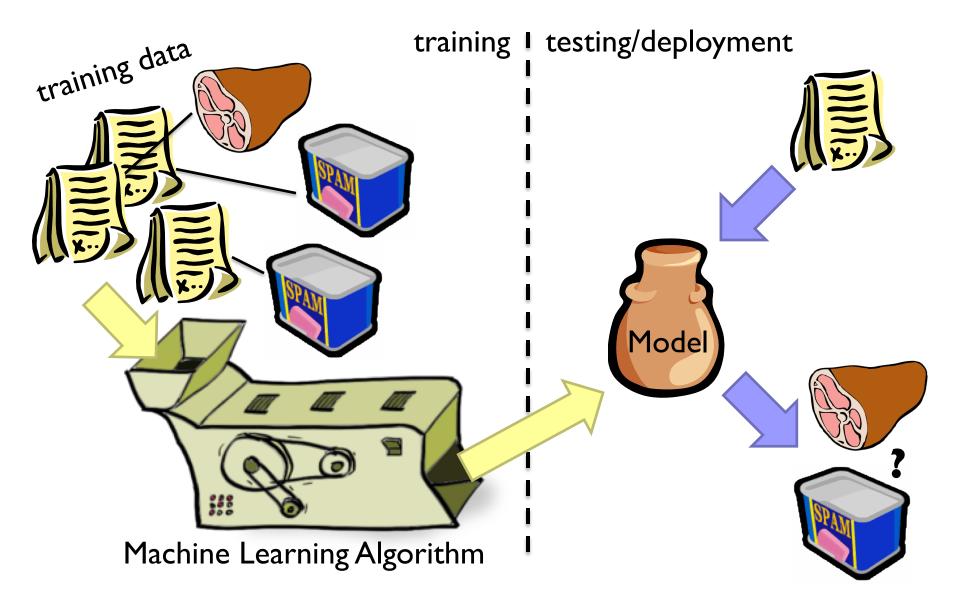
This is not meant to be an exhaustive treatment of machine learning!



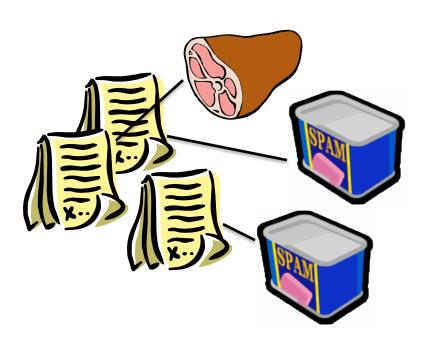
Applications

Spam detection Sentiment analysis Content (e.g., topic) classification Link prediction Document ranking Object recognition Fraud detection And much much more!

Supervised Machine Learning



Feature Representations



Who comes up with the features? How?

Objects are represented in terms of features:

"Dense" features: sender IP, timestamp, # of recipients, length of message, etc.

"Sparse" features: contains the term "viagra" in message, contains "URGENT" in subject, etc.

Applications

Spam detection

Sentiment analysis

Content (e.g., genre) classification

Link prediction

Document ranking

Object recognition

Fraud detection

And much much more!

Features are highly application-specific!

Components of a ML Solution

gradient descent, stochastic gradient descent, L-BFGS, etc.

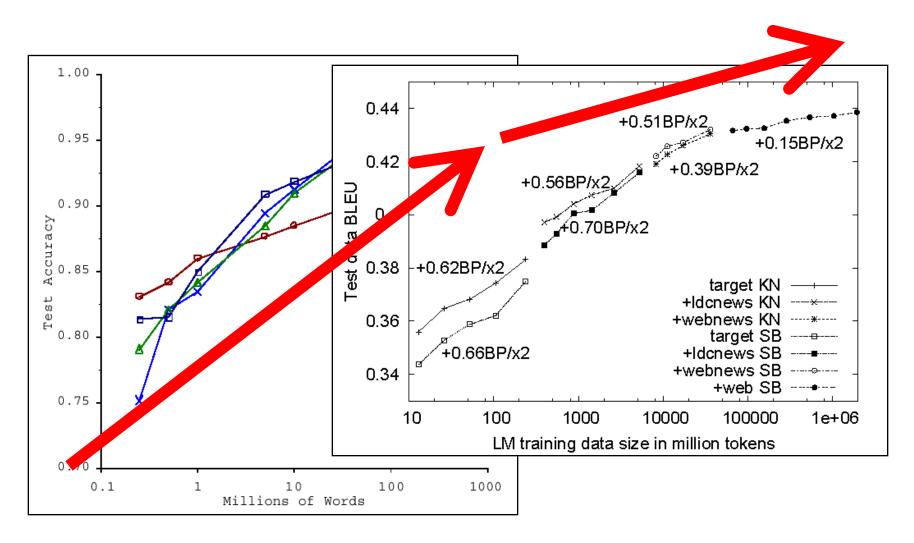
Data
Features
Model

logistic regression, naïve Bayes, SVM, random forests, perceptrons, neural networks, etc.

Optimization

What "matters" the most?

No data like more data!



Limits of Supervised Classification?

Why is this a big data problem?

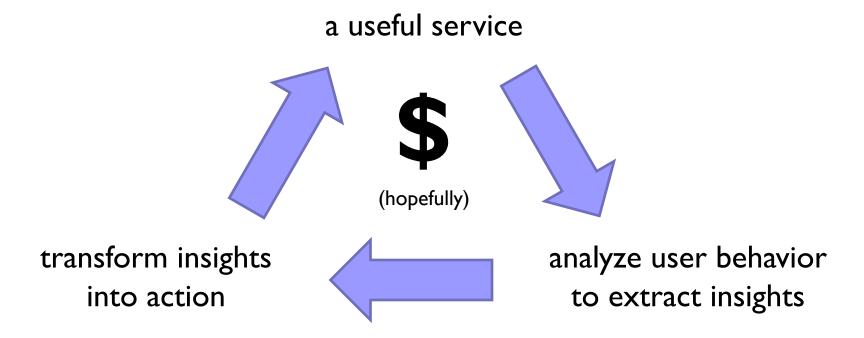
Isn't gathering labels a serious bottleneck?

Solutions

Crowdsourcing
Bootstrapping, semi-supervised techniques
Exploiting user behavior logs

The virtuous cycle of data-driven products

Virtuous Product Cycle



Google. Facebook. Twitter. Amazon. Uber.

data products

data science

What's the deal with neural networks?

Data
Features
Model
Optimization

Supervised Binary Classification

Restrict output label to be binary
Yes/No
1/0

Binary classifiers form primitive building blocks for multi-class problems...

Binary Classifiers as Building Blocks

Example: four-way classification

One vs. rest classifiers

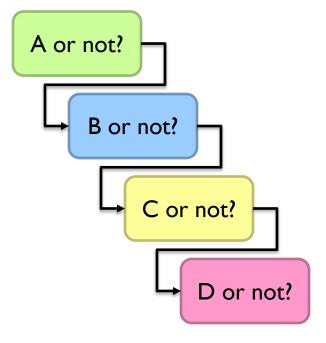
A or not?

B or not?

C or not?

D or not?

Classifier cascades



The Task

Given:
$$D = \{(\mathbf{x}_i, y_i)\}_i^n$$
 (sparse) feature vector $\mathbf{x}_i = [x_1, x_2, x_3, \dots, x_d]$ $y \in \{0, 1\}$

Induce: $f: X \to Y$

Such that loss is minimized

$$\frac{1}{n} \sum_{i=0}^{n} \ell(f(\mathbf{x}_i), y_i)$$

loss function

Typically, we consider functions of a parametric form:

$$\arg\min_{\theta} \frac{1}{n} \sum_{i=0}^{n} \ell(f(x_i; \theta), y_i)$$
 model parameters

Key insight: machine learning as an optimization problem! (closed form solutions generally not possible)

Gradient Descent: Preliminaries

Rewrite:

$$\operatorname{arg\,min}_{\theta} \frac{1}{n} \sum_{i=0}^{n} \ell(f(\mathbf{x}_i; \theta), y_i) \qquad \qquad \operatorname{arg\,min}_{\theta} L(\theta)$$

Compute gradient:

"Points" to fastest increasing "direction"

$$\nabla L(\theta) = \left[\frac{\partial L(\theta)}{\partial w_0}, \frac{\partial L(\theta)}{\partial w_1}, \dots \frac{\partial L(\theta)}{\partial w_d} \right]$$

So, at any point: *

$$b = a - \gamma \nabla L(a)$$

 $L(a) > L(b)$

Gradient Descent: Iterative Update

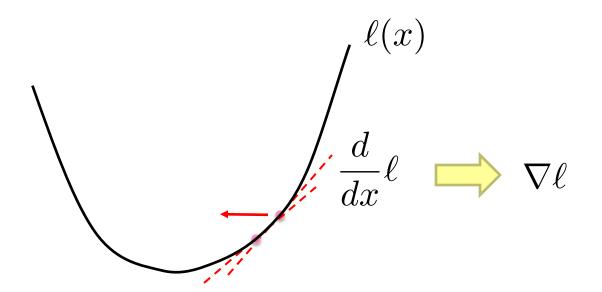
Start at an arbitrary point, iteratively update:

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla L(\theta^{(t)})$$

We have:

$$L(\theta^{(0)}) \ge L(\theta^{(1)}) \ge L(\theta^{(2)}) \dots$$

Intuition behind the math...



$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^n \nabla \ell(f(\mathbf{x}_i; \theta^{(t)}), y_i)$$
 New weights Old weights

Update based on gradient

Gradient Descent: Iterative Update

Start at an arbitrary point, iteratively update:

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla L(\theta^{(t)})$$

We have:

$$L(\theta^{(0)}) \ge L(\theta^{(1)}) \ge L(\theta^{(2)}) \dots$$

Lots of details:

Figuring out the step size

Getting stuck in local minima

Convergence rate

. . .

Gradient Descent

Repeat until convergence:

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathbf{x}_i; \theta^{(t)}), y_i)$$

Note, sometimes formulated as ascent but entirely equivalent



Even More Details...

Gradient descent is a "first order" optimization technique Often, slow convergence

Newton and quasi-Newton methods:

Intuition: Taylor expansion

$$f(x + \Delta x) = f(x) + f'(x)\Delta x + \frac{1}{2}f''(x)\Delta x^2$$

Requires the Hessian (square matrix of second order partial derivatives): impractical to fully compute



Logistic Regression: Preliminaries

Given:
$$D = \{(\mathbf{x}_i, y_i)\}_i^n$$

 $\mathbf{x}_i = [x_1, x_2, x_3, \dots, x_d]$
 $y \in \{0, 1\}$

Define:
$$f(\mathbf{x}; \mathbf{w}) : \mathbb{R}^d \to \{0, 1\}$$

$$f(\mathbf{x}; \mathbf{w}) = \begin{cases} 1 & \text{if } \mathbf{w} \cdot \mathbf{x} \ge t \\ 0 & \text{if } \mathbf{w} \cdot \mathbf{x} < t \end{cases}$$

Interpretation:
$$\ln\left[\frac{\Pr\left(y=1|\mathbf{x}\right)}{\Pr\left(y=0|\mathbf{x}\right)}\right] = \mathbf{w} \cdot \mathbf{x}$$

$$\ln\left[\frac{\Pr\left(y=1|\mathbf{x}\right)}{1-\Pr\left(y=1|\mathbf{x}\right)}\right] = \mathbf{w} \cdot \mathbf{x}$$

Relation to the Logistic Function

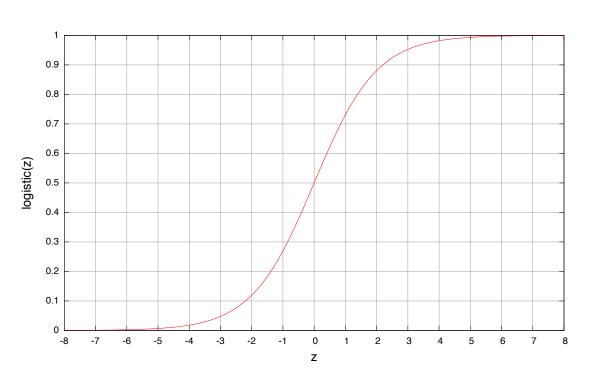
After some algebra:

$$\Pr\left(y=1|x\right) = \frac{e^{\mathbf{w} \cdot \mathbf{x}}}{1 + e^{\mathbf{w} \cdot \mathbf{x}}}$$

$$\Pr\left(y = 0 | x\right) = \frac{1}{1 + e^{\mathbf{w} \cdot \mathbf{x}}}$$

The logistic function:

$$f(z) = \frac{e^z}{e^z + 1}$$



Training an LR Classifier

Maximize the conditional likelihood:

$$\arg\max_{\mathbf{w}} \prod_{i=1}^{n} \Pr(y_i|\mathbf{x}_i,\mathbf{w})$$

Define the objective in terms of conditional *log* likelihood:

$$L(\mathbf{w}) = \sum_{i=1}^{n} \ln \Pr(y_i | \mathbf{x}_i, \mathbf{w})$$

We know: $y \in \{0, 1\}$

So:
$$Pr(y|x, w) = Pr(y = 1|x, w)^y Pr(y = 0|x, w)^{(1-y)}$$

Substituting:

$$L(\mathbf{w}) = \sum_{i=1}^{n} \left(y_i \ln \Pr(y_i = 1 | \mathbf{x}_i, \mathbf{w}) + (1 - y_i) \ln \Pr(y_i = 0 | \mathbf{x}_i, \mathbf{w}) \right)$$

LR Classifier Update Rule

Take the derivative:

$$L(\mathbf{w}) = \sum_{i=1}^{n} \left(y_i \ln \Pr(y_i = 1 | \mathbf{x}_i, \mathbf{w}) + (1 - y_i) \ln \Pr(y_i = 0 | \mathbf{x}_i, \mathbf{w}) \right)$$
$$\frac{\partial}{\partial \mathbf{w}} L(\mathbf{w}) = \sum_{i=0}^{n} \mathbf{x}_i \left(y_i - \Pr(y_i = 1 | \mathbf{x}_i, \mathbf{w}) \right)$$

General form of update rule:

$$\mathbf{w}^{(t+1)} \leftarrow \mathbf{w}^{(t)} + \gamma^{(t)} \nabla_{\mathbf{w}} L(\mathbf{w}^{(t)})$$

$$\nabla L(\mathbf{w}) = \left[\frac{\partial L(\mathbf{w})}{\partial w_0}, \frac{\partial L(\mathbf{w})}{\partial w_1}, \dots \frac{\partial L(\mathbf{w})}{\partial w_d} \right]$$

Final update rule:

$$\mathbf{w}_{i}^{(t+1)} \leftarrow \mathbf{w}_{i}^{(t)} + \gamma^{(t)} \sum_{j=0}^{n} x_{j,i} \Big(y_{j} - \Pr(y_{j} = 1 | \mathbf{x}_{j}, \mathbf{w}^{(t)}) \Big)$$

Lots more details...

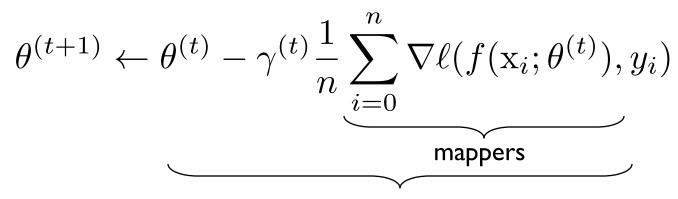
Regularization

Different loss functions

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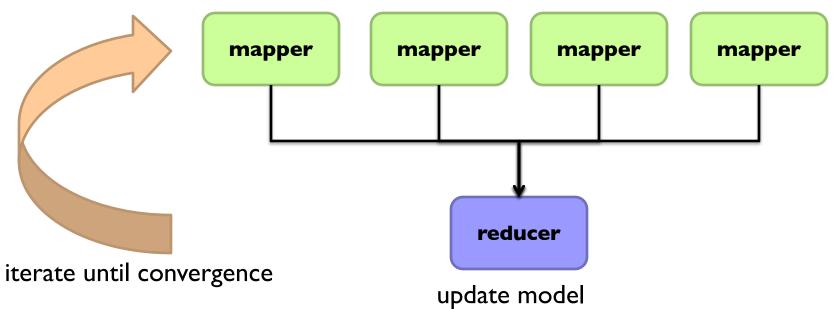
Want more details?
Take a real machine-learning course!

MapReduce Implementation



single reducer

compute partial gradient



Shortcomings

Hadoop is bad at iterative algorithms

High job startup costs
Awkward to retain state across iterations

High sensitivity to skew Iteration speed bounded by slowest task

Potentially poor cluster utilization

Must shuffle all data to a single reducer

Some possible tradeoffs

Number of iterations vs. complexity of computation per iteration E.g., L-BFGS: faster convergence, but more to compute

Spark Implementation

```
val points = spark.textFile(...).map(parsePoint).persist()
var w = // random initial vector
for (i <- 1 to ITERATIONS) {
 val gradient = points.map{ p =>
   p.x * (1/(1+exp(-p.y*(w dot p.x)))-1)*p.y
                                      What's the difference?
 w -= gradient
                        compute partial gradient
             mapper
                          mapper
                                      mapper
                                                  mapper
                                reducer
                             update model
```

