Big Data Infrastructure

Session 6: MapReduce – Data Mining

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Today's Agenda

- Clustering
- Classification

Clustering

Source: Wikipedia (Star cluster)

Problem Setup

- Arrange items into clusters
 - High similarity (low distance) between objects in the same cluster
 - Low similarity (high distance) between objects in different clusters
- Cluster labeling is a separate problem

Applications

- Exploratory analysis of large collections of objects
- Collection pre-processing for web search
- Image segmentation
- Recommender systems
- Cluster hypothesis in information retrieval
- Computational biology and bioinformatics
- Many more!

Distance Metrics

- I. Non-negativity: $d(x,y) \geq 0$
- 2. Identity:

$$d(x,y) = 0 \iff x = y$$

3. Symmetry:

$$d(x, y) = d(y, x)$$

4. Triangle Inequality

$$d(x,y) \leq d(x,z) + d(z,y)$$

Distance: Jaccard

- Given two sets A, B
- Jaccard similarity:

$$J(A, B) = \frac{|A \cap B|}{|A \cup B|}$$
$$d(A, B) = 1 - J(A, B)$$

Distance: Norms

• Given:
$$x = [x_1, x_2, \dots x_n]$$

 $y = [y_1, y_2, \dots y_n]$

• Euclidean distance (L₂-norm)

$$d(x, y) = \sqrt{\sum_{i=0}^{n} (x_i - y_i)^2}$$

• Manhattan distance (L₁-norm)

$$d(x, y) = \sum_{i=0}^{n} |x_i - y_i|$$

• L_r-norm

$$d(x, y) = \left[\sum_{i=0}^{n} |x_i - y_i|^r\right]^{1/r}$$

Distance: Cosine

• Given:
$$x = [x_1, x_2, \dots x_n]$$

 $y = [y_1, y_2, \dots y_n]$

• Idea: measure distance between the vectors

$$\cos \theta = \frac{\mathbf{x} \cdot \mathbf{y}}{|\mathbf{x}||\mathbf{y}|}$$

• Thus:

$$\operatorname{sim}(\mathbf{x}, \mathbf{y}) = \frac{\sum_{i=0}^{n} x_i y_i}{\sqrt{\sum_{i=0}^{n} x_i^2} \sqrt{\sum_{i=0}^{n} y_i^2}}$$
$$\operatorname{d}(\mathbf{x}, \mathbf{y}) = 1 - \operatorname{sim}(\mathbf{x}, \mathbf{y})$$

Distance: Hamming

- Given two bit vectors
- Hamming distance: number of elements which differ

Representations: Text

- Unigrams (i.e., words)
- Shingles = *n*-grams
 - At the word level
 - At the character level
- Feature weights
 - boolean
 - tf.idf
 - BM25
 - ...

Representations: Beyond Text

- For recommender systems:
 - Items as features for users
 - Users as features for items
- For graphs:
 - Adjacency lists as features for vertices
- With log data:
 - Behaviors (clicks) as features

Minhash

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Source: www.flickr.com/photos/rheinitz/6158837748/

Near-Duplicate Detection of Webpages

- What's the source of the problem?
 - Mirror pages (legit)
 - Spam farms (non-legit)
 - Additional complications (e.g., nav bars)
- Naïve algorithm:
 - Compute cryptographic hash for webpage (e.g., MD5)
 - Insert hash values into a big hash table
 - Compute hash for new webpage: collision implies duplicate
- What's the issue?
- Intuition:
 - Hash function needs to be tolerant of minor differences
 - High similarity implies higher probability of hash collision

Minhash

- Seminal algorithm for near-duplicate detection of webpages
 - Used by AltaVista
 - For details see Broder et al. (1997)
- Setup:
 - Documents (HTML pages) represented by shingles (*n*-grams)
 - Jaccard similarity: dups are pairs with high similarity

Preliminaries: Representation

• Sets:

- $A = \{e_1, e_3, e_7\}$
- $B = \{e_3, e_5, e_7\}$
- Can be equivalently expressed as matrices:

Element	Α	В
e _l	I	0
e ₂	0	0
e ₃	I	I
e ₄	0	0
e ₅	0	I
e ₆	0	0
e ₇	I	Ι

Preliminaries: Jaccard

Element	Α	В	
e _l	I	0	
e ₂	0	0	Let:
e ₃	Ι	I	M_{00} = # rows where both elements are 0
e ₄	0	0	$M_{II} = \#$ rows where both elements are I
e ₅	0	I.	$M_{01} = \#$ rows where A=0, B=1
e ₆	0	0	$M_{10} = \#$ rows where A=1, B=0
e ₇	Ι	I	

$$J(A,B) = \frac{M_{11}}{M_{01} + M_{10} + M_{11}}$$

Minhash

• Computing minhash

- Start with the matrix representation of the set
- Randomly permute the rows of the matrix
- minhash is the first row with a "one"

• Example:

$$h(A) = e_3 h(B) = e_5$$

Element	А	В	Element	А	В
e ₁	I	0	e ₆	0	0
e ₂	0	0	e ₂	0	0
e ₃	I	I	e ₅	0	I
e ₄	0	0	e ₃	I	I
e ₅	0	I.	e ₇	I	I
e ₆	0	0	e ₄	0	0
e ₇	I	I.	e,	I	0

Minhash and Jaccard

Element	Α	В	
e ₆	0	0	M ₀₀
e ₂	0	0	M ₀₀
e ₅	0	I	M ₀₁
e ₃	I	I	M ₁₁
e ₇	I	I	M ₁₁
e ₄	0	0	M ₀₀
e,	I	0	M ₁₀

$$P[h(A) = h(B)] = J(A, B)$$
$$\frac{M_{11}}{M_{01} + M_{10} + M_{11}} \qquad \frac{M_{11}}{M_{01} + M_{10} + M_{11}}$$

To Permute or Not to Permute?

- Permutations are expensive
- Interpret the hash value as the permutation
- Only need to keep track of the minimum hash value
 - Can keep track of multiple minhash values at once

Extracting Similar Pairs (LSH)

- We know: P[h(A) = h(B)] = J(A, B)
- Task: discover all pairs with similarity greater than S
- Algorithm:
 - For each object, compute its minhash value
 - Group objects by their hash values
 - Output all pairs within each group
- Analysis:
 - Probability we will discovered all pairs is s
 - Probability that any pair is invalid is (I s)
- What's the fundamental issue?

Two Minhash Signatures

- Task: discover all pairs with similarity greater than S
- Algorithm:
 - For each object, compute two minhash values and concatenate together into a signature
 - Group objects by their signatures
 - Output all pairs within each group
- Analysis:
 - Probability we will discovered all pairs is s²
 - Probability that any pair is invalid is $(1 s)^2$

k Minhash Signatures

- Task: discover all pairs with similarity greater than S
- Algorithm:
 - For each object, compute k minhash values and concatenate together into a signature
 - Group objects by their signatures
 - Output all pairs within each group
- Analysis:
 - Probability we will discovered all pairs is s^k
 - Probability that any pair is invalid is $(1 s)^k$
- What's the issue now?

n different k Minhash Signatures

- Task: discover all pairs with similarity greater than S
- Algorithm:
 - For each object, compute *n* sets *k* minhash values
 - For each set, concatenate k minhash values together
 - Within each set:
 - Group objects by their signatures
 - Output all pairs within each group
 - De-dup pairs
- Analysis:
 - Probability we will miss a pair is $(I s^k)^n$
 - Probability that any pair is invalid is $n(1 s)^k$

Practical Notes

• In some cases, checking all candidate pairs may be possible

- Time cost is small relative to everything else
- Easy method to discard false positives
- Most common practical implementation:
 - Generate *M* minhash values, randomly select *k* of them *n* times
 - Reduces amount of hash computations needed
- Determining "authoritative" version is non-trivial

MapReduce Implementation

• Map over objects:

- Generate *M* minhash values, randomly select *k* of them *n* times
- Each draw yields a signature: emit as intermediate key, value is object id
- Shuffle/sort:
- Reduce:
 - Receive all object ids with same signature, emit clusters
- Second pass to de-dup and group clusters

General Clustering Approaches

- Hierarchical
- K-Means
- Gaussian Mixture Models

Hierarchical Agglomerative Clustering

- Start with each document in its own cluster
- Until there is only one cluster:
 - Find the two clusters c_i and c_j , that are most similar
 - Replace c_i and c_j with a single cluster $c_i \cup c_j$
- The history of merges forms the hierarchy

HAC in Action



Cluster Merging

- Which two clusters do we merge?
- What's the similarity between two clusters?
 - Single Link: similarity of two most similar members
 - Complete Link: similarity of two least similar members
 - Group Average: average similarity between members

Link Functions

• Single link:

• Uses maximum similarity of pairs:

$$\sin(c_i, c_j) = \max_{x \in c_i, y \in c_j} \sin(x, y)$$

• Can result in "straggly" (long and thin) clusters due to chaining effect

• Complete link:

• Use minimum similarity of pairs:

$$\sin(c_i, c_j) = \min_{x \in c_i, y \in c_j} \sin(x, y)$$

• Makes more "tight" spherical clusters

MapReduce Implementation

• What's the inherent challenge?

K-Means Algorithm

- Let d be the distance between documents
- Define the centroid of a cluster to be:

$$\mu(c) = \frac{1}{|c|} \sum_{\mathbf{x} \in c} \mathbf{x}$$

- Select k random instances $\{s_1, s_2, \dots, s_k\}$ as seeds.
- Until clusters converge:
 - Assign each instance x_i to the cluster c_i such that $d(x_i, s_i)$ is minimal
 - Update the seeds to the centroid of each cluster
 - For each cluster c_j , $s_j = \mu(c_j)$

K-Means Clustering Example



Pick seeds
Reassign clusters
Compute centroids
Reassign clusters
Compute centroids
Reassign clusters
Converged!

Basic MapReduce Implementation

1: class MAPPER

- 2: **method** CONFIGURE()
- 3: $c \leftarrow \text{LOADCLUSTERS}()$
- 4: **method** MAP(id i, point p)
- 5: $n \leftarrow \text{NEARESTCLUSTERID}(\text{clusters } c, \text{ point } p)$

```
p \leftarrow \text{ExtendPoint}(\text{point } p) \longleftarrow  (Just a clever way to keep
6:
```

EMIT(clusterid n, point p) 7:

track of denominator)

- 1: class Reducer.
- 2: **method** REDUCE(clusterid *n*, points $[p_1, p_2, \ldots]$)
- $s \leftarrow \text{INITPOINTSUM}()$ 3:
- 4: for all point $p \in$ points do

```
5:
            s \leftarrow s + p
```

- 6: $m \leftarrow \text{COMPUTECENTROID}(\text{point } s)$
- EMIT(clusterid n, centroid m) 7:

MapReduce Implementation w/ IMC

- 1: **class** Mapper
- 2: **method** CONFIGURE()
- 3: $c \leftarrow \text{LOADCLUSTERS}()$
- 4: $H \leftarrow \text{INITASSOCIATIVEARRAY}()$
- 5: method MAP(id i, point p)
- 6: $n \leftarrow \text{NEARESTCLUSTERID}(\text{clusters } c, \text{ point } p)$
- 7: $p \leftarrow \text{ExtendPoint}(\text{point } p)$
- 8: $H\{n\} \leftarrow H\{n\} + p$
- 9: method CLOSE()
- 10: for all clusterid $n \in H$ do
- 11: EMIT(clusterid n, point $H\{n\}$)
 - 1: **class** Reducer
 - 2: method REDUCE(clusterid n, points $[p_1, p_2, \ldots]$)
 - 3: $s \leftarrow \text{INITPOINTSUM}()$
 - 4: for all point $p \in \text{points}$ do
 - 5: $s \leftarrow s + p$
 - 6: $m \leftarrow \text{COMPUTECENTROID}(\text{point } s)$
 - 7: EMIT(clusterid n, centroid m)
Implementation Notes

• Standard setup of iterative MapReduce algorithms

- Driver program sets up MapReduce job
- Waits for completion
- Checks for convergence
- Repeats if necessary
- Must be able keep cluster centroids in memory
 - With large k, large feature spaces, potentially an issue
 - Memory requirements of centroids grow over time!
- Variant: *k*-medoids

Clustering w/ Gaussian Mixture Models

- Model data as a mixture of Gaussians
- Given data, recover model parameters



Gaussian Distributions

• Univariate Gaussian (i.e., Normal):

$$p(x;\mu,\sigma^2) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{1}{2\sigma^2}(x-\mu)^2\right)$$

- A random variable with such a distribution we write as: $x \sim \mathcal{N}(\mu, \sigma^2)$
- Multivariate Gaussian:

$$p(\mathbf{x};\mu,\Sigma) = \frac{1}{(2\pi)^{n/2} |\Sigma|^{1/2}} \exp\left(-\frac{1}{2}(\mathbf{x}-\mu)^T \Sigma^{-1}(\mathbf{x}-\mu)\right)$$

- A vector-value random variable with such a distribution we write as: $\mathbf{x}\sim\mathcal{N}(\mu,\Sigma)$

Univariate Gaussian



Source: Wikipedia (Normal Distribution)

Multivariate Gaussians





Source: Lecture notes by Chuong B. Do (IIT Delhi)

Gaussian Mixture Models

• Model parameters

- Number of components: K
- "Mixing" weight vector: $\boldsymbol{\pi}$
- For each Gaussian, mean and covariance matrix: $\mu_{1:K}$ $\Sigma_{1:K}$
- Varying constraints on co-variance matrices
 - Spherical vs. diagonal vs. full
 - Tied vs. untied

Learning for Simple Univariate Case

• Problem setup:

- Given number of components: K
- Given points: $x_{1:N}$
- Learn parameters: $\pi, \mu_{1:K}, \sigma_{1:K}^2$
- Model selection criterion: maximize likelihood of data
 - Introduce indicator variables:

$$z_{n,k} = \begin{cases} 1 & \text{if } x_n \text{ is in cluster } k \\ 0 & \text{otherwise} \end{cases}$$

• Likelihood of the data:

 $p(x_{1:N}, z_{1:N,1:K} | \mu_{1:K}, \sigma_{1:K}^2, \pi)$

EM to the Rescue!

• We're faced with this:

 $p(x_{1:N}, z_{1:N,1:K} | \mu_{1:K}, \sigma_{1:K}^2, \pi)$

- It'd be a lot easier if we knew the z's!
- Expectation Maximization
 - Guess the model parameters
 - E-step: Compute posterior distribution over latent (hidden) variables given the model parameters
 - M-step: Update model parameters using posterior distribution computed in the E-step
 - Iterate until convergence



"I THINK YOU SHOULD BE MORE EXPLICIT HERE IN STEP TWO."

EM for Univariate GMMs

- Initialize: $\pi, \mu_{1:K}, \sigma_{1:K}^2$
- Iterate:
 - E-step: compute expectation of z variables

$$\mathbb{E}[z_{n,k}] = \frac{\mathcal{N}(x_n | \mu_k, \sigma_k^2) \cdot \pi_k}{\sum_{k'} \mathcal{N}(x_n | \mu_{k'}, \sigma_{k'}^2) \cdot \pi_{k'}}$$

• M-step: compute new model parameters

$$\pi_k = \frac{1}{N} \sum_n z_{n,k}$$
$$\mu_k = \frac{1}{\sum_n z_{n,k}} \sum_n z_{n,k} \cdot x_n$$
$$\sigma_k^2 = \frac{1}{\sum_n z_{n,k}} \sum_n z_{n,k} ||x_n - \mu_k||^2$$

MapReduce Implementation

 \mathbf{Map} $\mathbb{E}[z_{n,k}] = \frac{\mathcal{N}(x_n | \mu_k, \sigma_k^2) \cdot \pi_k}{\sum_{k'} \mathcal{N}(x_n | \mu_{k'}, \sigma_{k'}^2) \cdot \pi_{k'}}$



Reduce

$$\pi_k = \frac{1}{N} \sum_n z_{n,k}$$
$$\mu_k = \frac{1}{\sum_n z_{n,k}} \sum_n z_{n,k} \cdot x_n$$
$$\sigma_k^2 = \frac{1}{\sum_n z_{n,k}} \sum_n z_{n,k} ||x_n - \mu_k||^2$$

K-Means vs. GMMs

K-Means

GMM

Мар

Compute distance of points to centroids

E-step: compute expectation of z indicator variables

Reduce Recompute new centroids

M-step: update values of model parameters

Summary

- Hierarchical clustering
 - Difficult to implement in MapReduce
- K-Means
 - Straightforward implementation in MapReduce
- Gaussian Mixture Models
 - Implementation conceptually similar to k-means, more "bookkeeping"

Classification

Source: Wikipedia (Sorting)

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Supervised Machine Learning

- The generic problem of function induction given sample instances of input and output
 - Classification: output draws from finite discrete labels
 - Regression: output is a continuous value
- Focus here on supervised classification
 - Suffices to illustrate large-scale machine learning

This is not meant to be an exhaustive treatment of machine learning!

Applications

- Spam detection
- Content (e.g., movie) classification
- POS tagging
- Friendship recommendation
- Document ranking
- Many, many more!

Supervised Binary Classification

- Restrict output label to be *binary*
 - Yes/No
 - 1/0
- Binary classifiers form a primitive building block for multi-class problems
 - One vs. rest classifier ensembles
 - Classifier cascades

Limits of Supervised Classification?

- Why is this a big data problem?
 - Isn't gathering labels a serious bottleneck?
- Solution: user behavior logs
 - Learning to rank
 - Computational advertising
 - Link recommendation
- The virtuous cycle of data-driven products

The Task

• Given $D = \{(x_i, y_i)\}_i^n$ (sparse) feature vector $x_i = [x_1, x_2, x_3, \dots, x_d]$ $y \in \{0, 1\}$

- Induce $f: X \to Y$
 - Such that loss is minimized

$$\frac{1}{n} \sum_{i=0}^{n} \ell(f(\mathbf{x}_i), y_i)$$

• Typically, consider functions of a parametric form:

$$\arg\min_{\theta} \frac{1}{n} \sum_{i=0}^{n} \ell(f(x_i; \theta), y_i) \qquad \qquad \text{model parameters}$$

Key insight: machine learning as an optimization problem! (closed form solutions generally not possible)

Gradient Descent: Preliminaries

• Rewrite:

$$\arg\min_{\theta} \frac{1}{n} \sum_{i=0}^{n} \ell(f(\mathbf{x}_i; \theta), y_i) \quad \arg\min_{\theta} L(\theta)$$

- Compute gradient:
 - "Points" to fastest increasing "direction"

$$\nabla L(\theta) = \left[\frac{\partial L(\theta)}{\partial w_0}, \frac{\partial L(\theta)}{\partial w_1}, \dots \frac{\partial L(\theta)}{\partial w_d}\right]$$

• So, at any point: *

$$b = a - \gamma \nabla L(a)$$
$$L(a) \ge L(b)$$



Gradient Descent: Iterative Update

• Start at an arbitrary point, iteratively update:

 $\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla L(\theta^{(t)})$

• We have:

 $L(\theta^{(0)}) \ge L(\theta^{(1)}) \ge L(\theta^{(2)}) \dots$

- Lots of details:
 - Figuring out the step size
 - Getting stuck in local minima
 - Convergence rate

• ...

Gradient Descent

Repeat until convergence:

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathbf{x}_i; \theta^{(t)}), y_i)$$

Intuition behind the math...



$$\begin{aligned} \theta^{(t+1)} &\leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathbf{x}_i; \theta^{(t)}), y_i) \\ \text{New weights} \quad \text{Old weights} \end{aligned}$$

Update based on gradient



Gradient Descent

 $\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathbf{x}_i; \theta^{(t)}), y_i)$

Lots More Details...

- Gradient descent is a "first order" optimization technique
 - Often, slow convergence
 - Conjugate techniques accelerate convergence
- Newton and quasi-Newton methods:
 - Intuition: Taylor expansion

$$f(x + \Delta x) = f(x) + f'(x)\Delta x + \frac{1}{2}f''(x)\Delta x^2$$

• Requires the Hessian (square matrix of second order partial derivatives): impractical to fully compute

Logistic Regression

Logistic Regression: Preliminaries

• Given
$$D = \{(x_i, y_i)\}_i^n$$

 $x_i = [x_1, x_2, x_3, \dots, x_d]$
 $y \in \{0, 1\}$

• Let's define:

$$f(\mathbf{x}; \mathbf{w}) : \mathbb{R}^d \to \{0, 1\}$$
$$f(\mathbf{x}; \mathbf{w}) = \begin{cases} 1 \text{ if } \mathbf{w} \cdot \mathbf{x} \ge t\\ 0 \text{ if } \mathbf{w} \cdot \mathbf{x} < t \end{cases}$$

• Interpretation:

$$\ln \left[\frac{\Pr(y=1|\mathbf{x})}{\Pr(y=0|\mathbf{x})} \right] = \mathbf{w} \cdot \mathbf{x}$$
$$\ln \left[\frac{\Pr(y=1|\mathbf{x})}{1 - \Pr(y=1|\mathbf{x})} \right] = \mathbf{w} \cdot \mathbf{x}$$

Relation to the Logistic Function

• After some algebra:

$$\Pr(y = 1|x) = \frac{e^{\mathbf{w} \cdot \mathbf{x}}}{1 + e^{\mathbf{w} \cdot \mathbf{x}}}$$
$$\Pr(y = 0|x) = \frac{1}{1 + e^{\mathbf{w} \cdot \mathbf{x}}}$$

• The logistic function:

$$f(z) = \frac{e^z}{e^z + 1}$$



Training an LR Classifier

• Maximize the conditional likelihood:

$$\arg\max_{\mathbf{w}}\prod_{i=1}^{n}\Pr(y_i|\mathbf{x}_i,\mathbf{w})$$

• Define the objective in terms of conditional log likelihood:

$$L(\mathbf{w}) = \sum_{i=1}^{n} \ln \Pr(y_i | \mathbf{x}_i, \mathbf{w})$$

• We know
$$y \in \{0,1\}$$
 so:

$$\Pr(y|\mathbf{x}, \mathbf{w}) = \Pr(y = 1|\mathbf{x}, \mathbf{w})^{y} \left[1 - \Pr(y = 0|\mathbf{x}, \mathbf{w})\right]^{(1-y)}$$

• Substituting:

$$L(\mathbf{w}) = \sum_{i=1}^{n} \left(y_i \ln \Pr(y_i = 1 | \mathbf{x}_i, \mathbf{w}) + (1 - y_i) \ln \Pr(y_i = 0 | \mathbf{x}_i, \mathbf{w}) \right)$$

LR Classifier Update Rule

• Take the derivative:

$$L(\mathbf{w}) = \sum_{i=1}^{n} \left(y_i \ln \Pr(y_i = 1 | \mathbf{x}_i, \mathbf{w}) + (1 - y_i) \ln \Pr(y_i = 0 | \mathbf{x}_i, \mathbf{w}) \right)$$
$$\frac{\partial}{\partial \mathbf{w}} L(\mathbf{w}) = \sum_{i=0}^{n} \mathbf{x}_i \left(y_i - \Pr(y_i = 1 | \mathbf{x}_i, \mathbf{w}) \right)$$

• General form for update rule:

$$\mathbf{w}^{(t+1)} \leftarrow \mathbf{w}^{(t)} + \gamma^{(t)} \nabla_{\mathbf{w}} L(\mathbf{w}^{(t)})$$
$$\nabla L(\mathbf{w}) = \left[\frac{\partial L(\mathbf{w})}{\partial w_0}, \frac{\partial L(\mathbf{w})}{\partial w_1}, \dots, \frac{\partial L(\mathbf{w})}{\partial w_d}\right]$$

• Final update rule:

$$\mathbf{w}_{i}^{(t+1)} \leftarrow \mathbf{w}_{i}^{(t)} + \gamma^{(t)} \sum_{j=0}^{n} x_{j,i} \Big(y_{j} - \Pr(y_{j} = 1 | \mathbf{x}_{j}, \mathbf{w}^{(t)}) \Big)$$

Lots more details...

- Regularization
- Different loss functions

o ...

Want more details? Take a real machine-learning course!

MapReduce Implementation



Shortcomings

- Hadoop is bad at iterative algorithms
 - High job startup costs
 - Awkward to retain state across iterations
- High sensitivity to skew
 - Iteration speed bounded by slowest task
- Potentially poor cluster utilization
 - Must shuffle all data to a single reducer
- Some possible tradeoffs
 - Number of iterations vs. complexity of computation per iteration
 - E.g., L-BFGS: faster convergence, but more to compute

Gradient Descent

Source: Wikipedia (Hills)
Stochastic Gradient Descent

rce: Wikipedia (Water Slide)

Batch vs. Online

Gradient Descent

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathbf{x}_i; \theta^{(t)}), y_i)$$

"batch" learning: update model after considering all training instances

Stochastic Gradient Descent (SGD)

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla \ell(f(\mathbf{x}; \theta^{(t)}), y)$$

"online" learning: update model after considering each (randomly-selected) training instance

In practice... just as good!

Practical Notes

- Most common implementation:
 - Randomly shuffle training instances
 - Stream instances through learner
- Single vs. multi-pass approaches
- "Mini-batching" as a middle ground between batch and stochastic gradient descent

We've solved the iteration problem! What about the single reducer problem?

Ensembles

-

THE OWNER WATER

Ensemble Learning

- Learn multiple models, combine results from different models to make prediction
- Why does it work?
 - If errors uncorrelated, multiple classifiers being wrong is less likely
 - Reduces the variance component of error
- A variety of different techniques:
 - Majority voting
 - Simple weighted voting:

$$y = \arg \max_{y \in Y} \sum_{k=1}^{n} \alpha_k p_k(y|\mathbf{x})$$

Model averaging

Practical Notes

- Common implementation:
 - Train classifiers on different input partitions of the data
 - Embarassingly parallel!
- Contrast with bagging
- Contrast with boosting

MapReduce Implementation

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla \ell(f(\mathbf{x}; \theta^{(t)}), y)$$



MapReduce Implementation: Details

- Shuffling/resort training instances before learning
- Two possible implementations:
 - Mappers write model out as "side data"
 - Mappers emit model as intermediate output

Sentiment Analysis Case Study

Lin and Kolcz, SIGMOD 2012

• Binary polarity classification: {positive, negative} sentiment

- Independently interesting task
- Illustrates end-to-end flow
- Use the "emoticon trick" to gather data
- o Data
 - Test: 500k positive/500k negative tweets from 9/1/2011
 - Training: {Im, I0m, I00m} instances from before (50/50 split)
- Features: Sliding window byte-4grams
- Models:
 - Logistic regression with SGD (L2 regularization)
 - Ensembles of various sizes (simple weighted voting)

Diminishing returns...



Takeaway Lesson

- Big data "recipe" for problem solving
 - Simple technique
 - Simple features
 - Lots of data
- Usually works very well!

Today's Agenda

- Clustering
- Classification

Questions?

Source: Wikipedia (Japanese rock garden)